

T = 0 Myr

Gas



T = 0 Myr

Stars



face on view

face on view

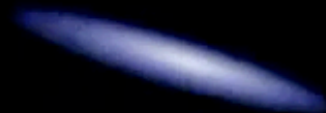
T = 0 Myr

Gas



T = 0 Myr

Stars



edge on view

edge on view

Kepler potential: $\phi(r) = -\frac{GM}{r}$

Plummer model: $\phi_P(r) = -\frac{GM}{(r^2+a^2)^{1/2}}$

Kuzmin disk: $\phi_K(R, z) = -\frac{GM}{(R^2+(a+|z|)^2)^{1/2}}$

Miyamoto disk: $\phi_M(R, z) = -\frac{GM}{\left(R^2+(a+\sqrt{z^2+b^2})^2\right)^{1/2}}$

Logarithmic: $\phi_L(R) = \frac{1}{2}v_0^2 \ln\left(R_c^2 + \frac{R^2}{a^2}\right)$
 $\phi_L(R, z) = \frac{1}{2}v_0^2 \ln\left(R_c^2 + \frac{R^2}{a^2} + \frac{z^2}{b^2}\right)$
(etc.)

Phase-space distribution function $f(\vec{x}, \vec{v})$:

$$n(\vec{x}) = \int_{-\infty}^{\infty} f(\vec{x}, \vec{v}) d^3 v$$

$$n \vec{u}(\vec{x}) = \int_{-\infty}^{\infty} \vec{v} f(\vec{x}, \vec{v}) d^3 v$$

$$n \sigma^2(\vec{x}) = \int_{-\infty}^{\infty} (\vec{v} - \vec{u})^2 f(\vec{x}, \vec{v}) d^3 v$$

Jeans theorem: $f(I_1, I_2, \dots)$ gives self-consistent solution

Plummer model: $f(E) = A(-E)^{7/2} \quad (E < 0)$

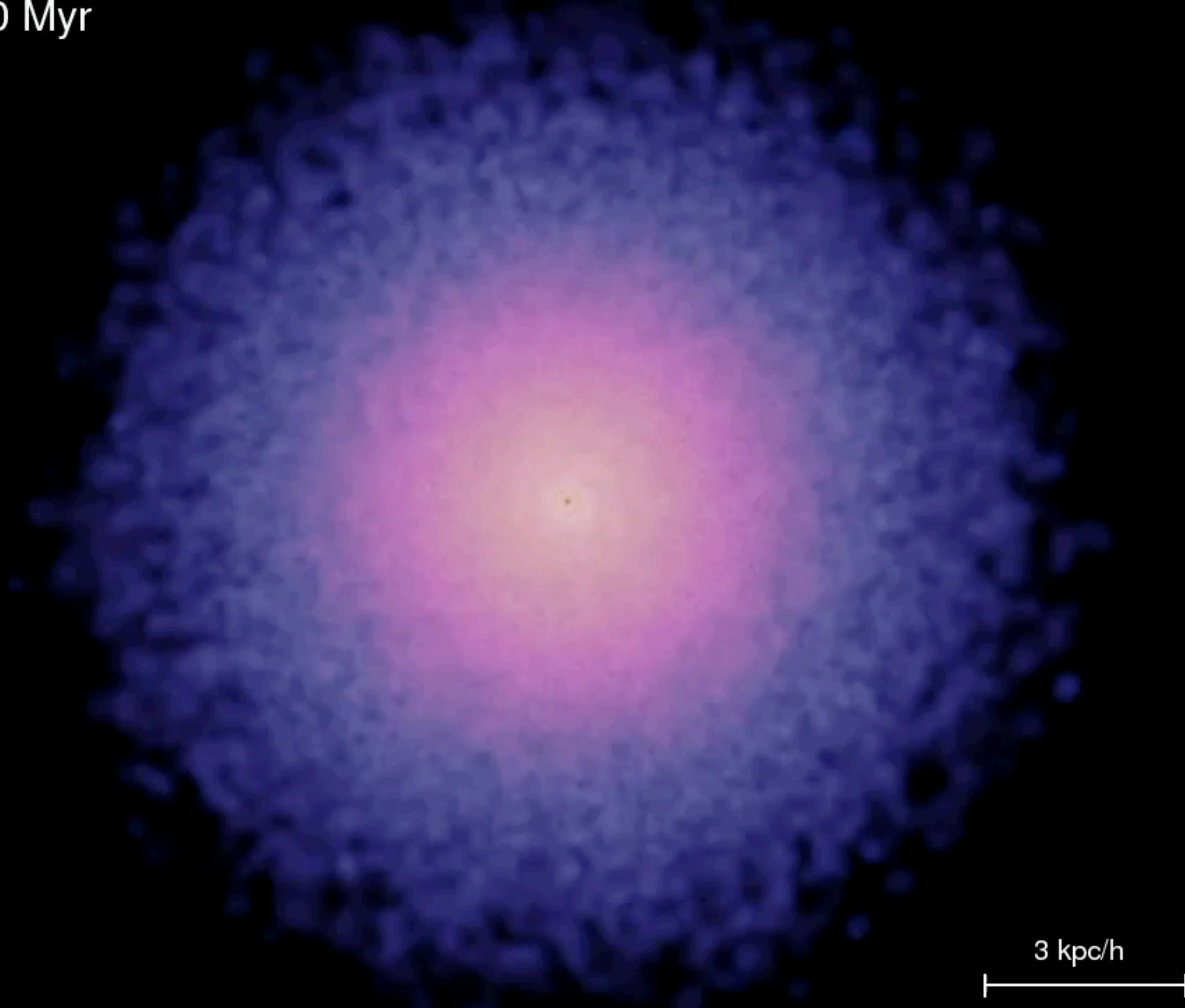
Isothermal model: $f(E) = A e^{-E/kT}$

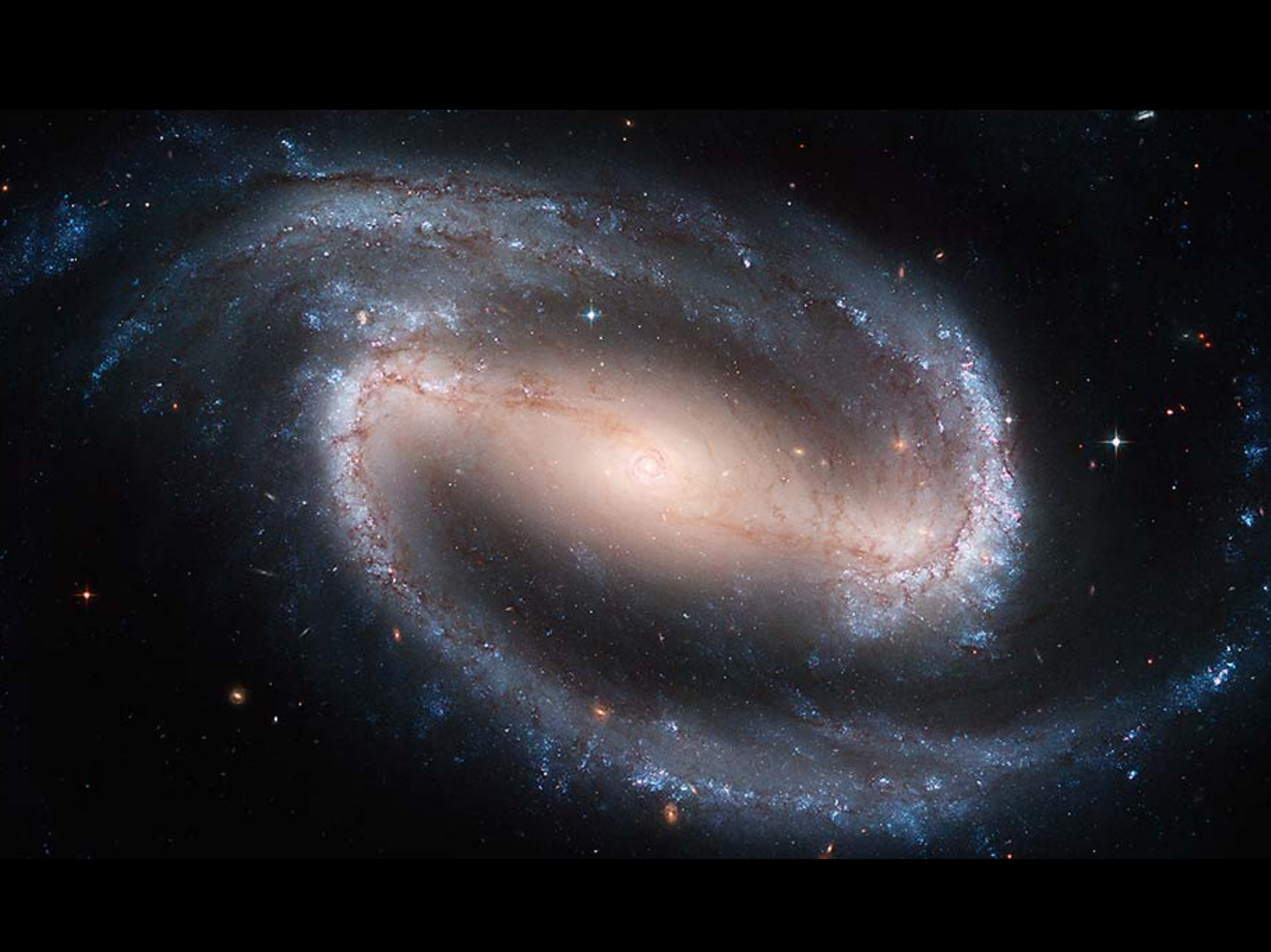
Lowered isothermal: $f(E) = A (e^{-E/kT} - 1)$

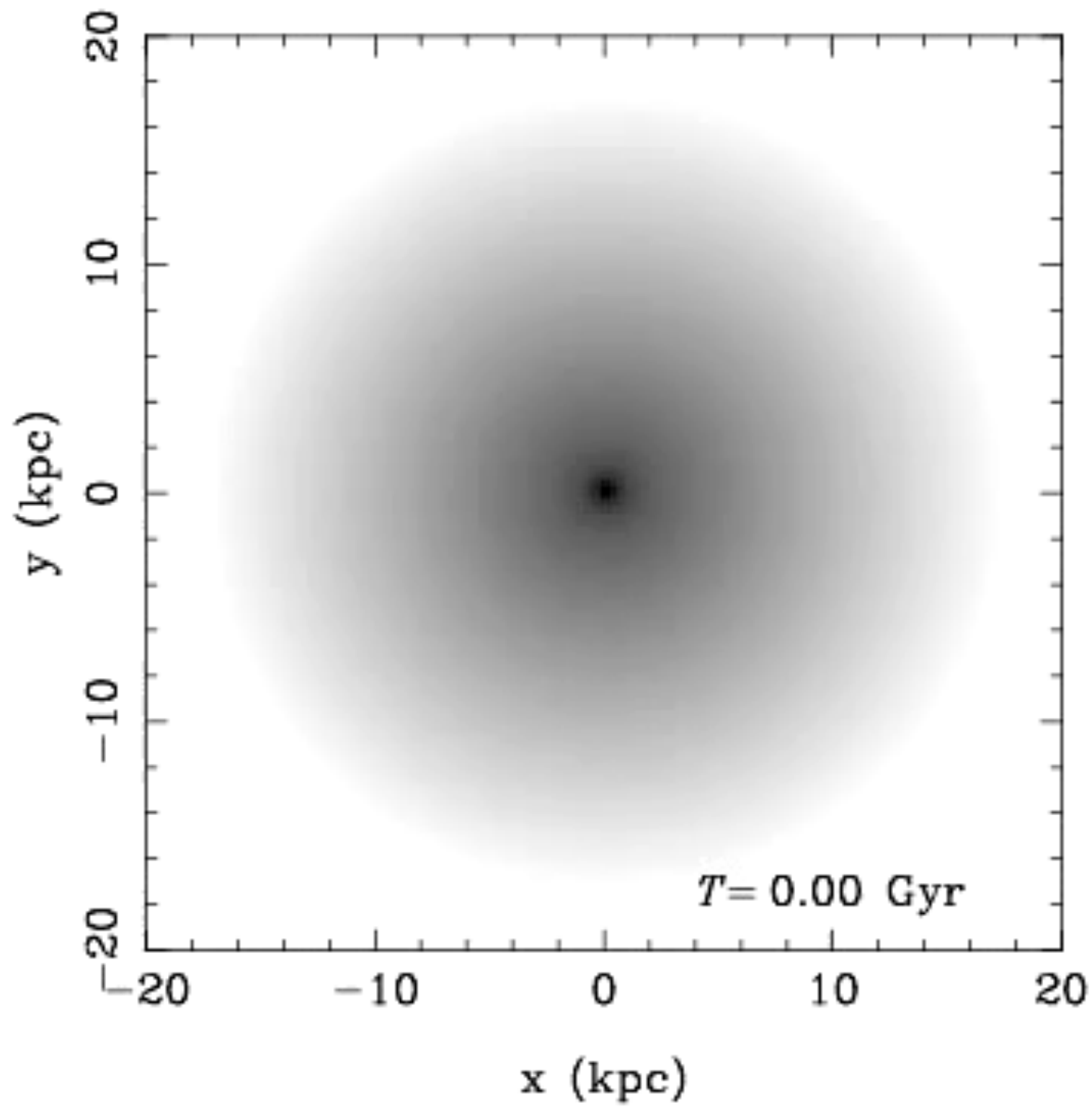
Anisotropy: $f(E, J) = A (e^{-E/kT} - 1) e^{-J^2/2r_a^2 kT}$



$T = 0$ Myr







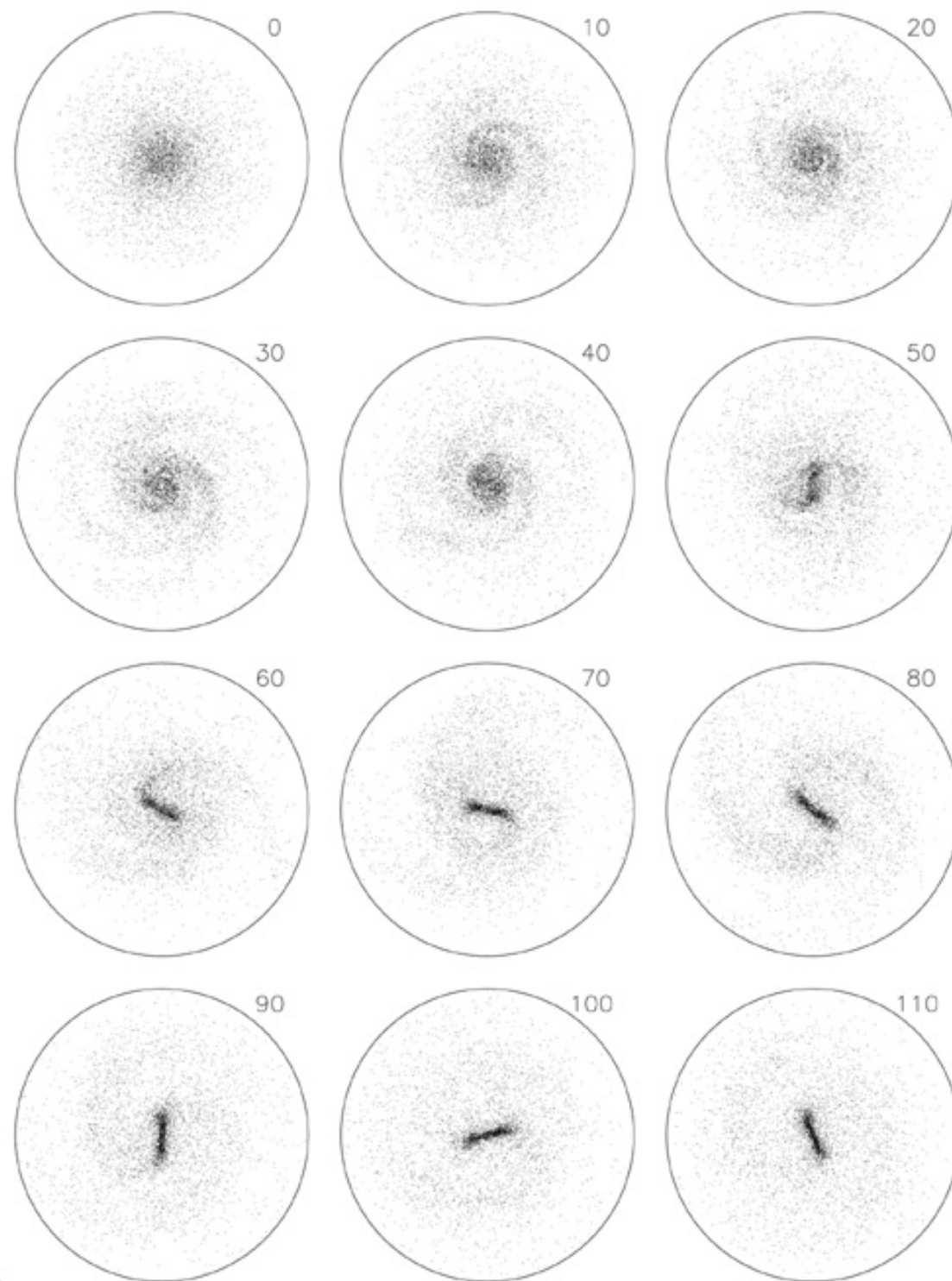
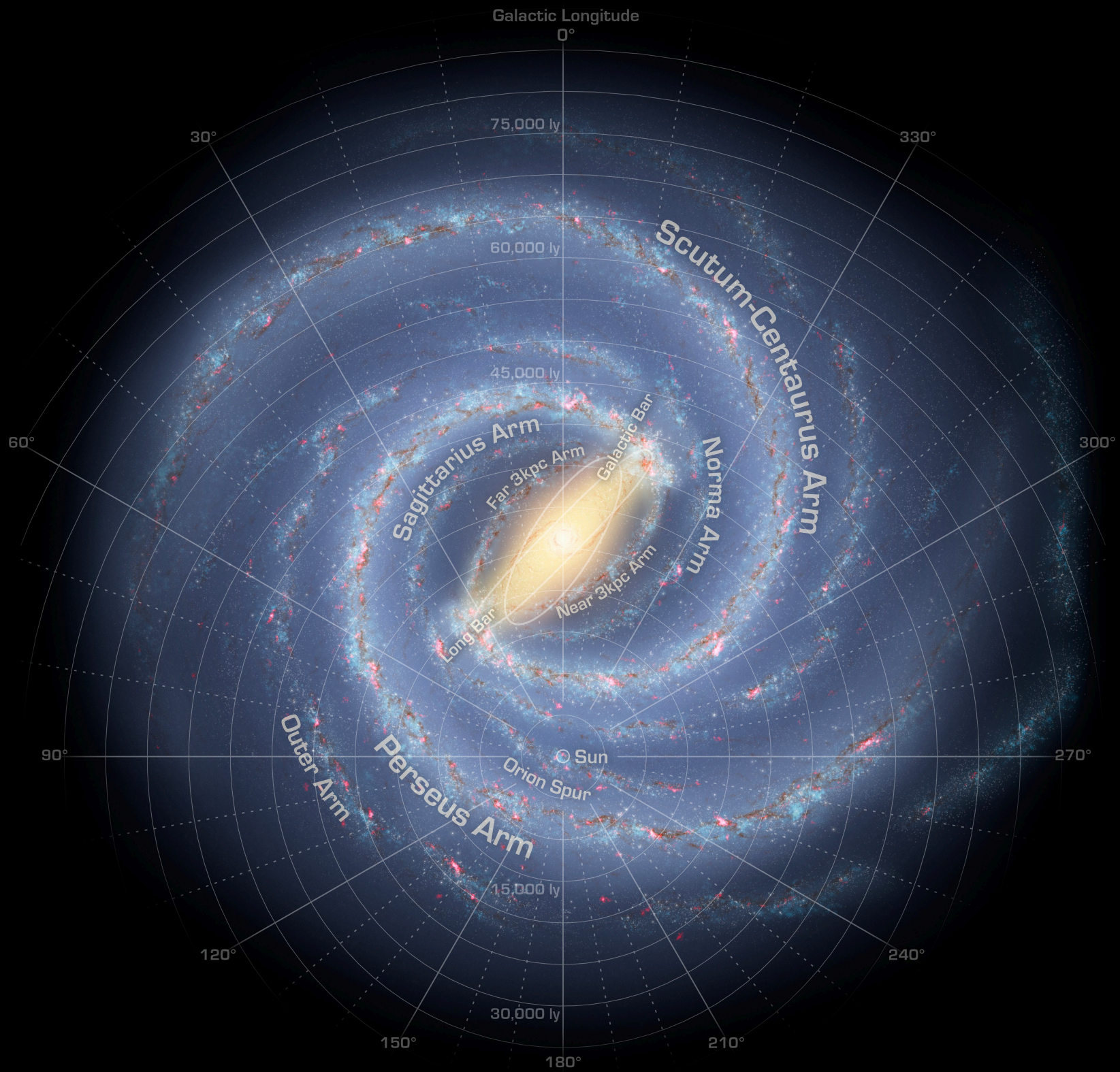


Fig 5.31 (J.Sellwood) 'Galaxies in the Universe' Sparke/Gallagher CUP 2007



$$\omega^2 = v_s^2 k^2$$

$$\omega^2 = v_s^2 k^2 - 4\pi G\rho$$

$$\omega^2 = v_s^2 k^2 - 4\pi G\rho + 4\Omega^2$$

$$\omega^2 = v_s^2 k^2 + 4\pi G\rho$$

$$\omega^2 = v_s^2 k^2 - 2\pi G\Sigma|k| + 4\Omega^2$$







