## PHYS 325: Computational Physics III

Winter 2023

Exercise 3.2

1. Use Monte-Carlo integration to estimate the area and mass of the two-dimensional region (x, y) defined by  $x^2 + 4y^2 < 1$ ,  $y^2 < x$ , and x + y < 0.5. The surface density of the material in the region is  $\sigma(x, y) = x^2 + y^2$ . Perform your calculation with  $N = 10^4$  and  $N = 10^6$  random points in the region under consideration. What are the estimated errors in each calculation?