

Homework 7

Chapter 22

Problem 6. A proton moves with a velocity of $\mathbf{v} = (2\hat{\mathbf{i}} - 4\hat{\mathbf{j}} + \hat{\mathbf{k}})$ m/s in a region in which the magnetic field is $\mathbf{B} = (\hat{\mathbf{i}} + 2\hat{\mathbf{j}} - 3\hat{\mathbf{k}})$ T. What is the magnitude of the magnetic force this charge experiences?

$$\mathbf{F} = q\mathbf{v} \times \mathbf{B} = q \begin{vmatrix} \hat{\mathbf{i}} & \hat{\mathbf{j}} & \hat{\mathbf{k}} \\ 2 & -4 & 1 \\ 1 & 2 & -3 \end{vmatrix} = q[\hat{\mathbf{i}}(12 - 2) - \hat{\mathbf{j}}(-6 - 1) + \hat{\mathbf{k}}(4 - (-4))] = q(10\hat{\mathbf{i}} + 7\hat{\mathbf{j}} + 8\hat{\mathbf{k}}) \quad (1)$$

$$|\mathbf{F}| = q\sqrt{10^2 + 7^2 + 8^2} = 2.34 \cdot 10^{-18} \text{ N} \quad (2)$$

Problem 8. An electron moves in a circular path perpendicular to a constant magnetic field of magnitude $B = 1.00$ mT. The angular momentum of the electron about the center of the circle is $L = 4.00 \cdot 10^{-25}$ Js. Determine (a) the radius of the circular path and (b) the speed of the electron.

Angular momentum is defined as

$$\mathbf{L} = \mathbf{r} \times \mathbf{p} = m\mathbf{r} \times \mathbf{v}, \quad (3)$$

which for circular orbits reduces to

$$L = mrv, \quad (4)$$

because \mathbf{r} and \mathbf{v} are perpendicular.

We also have

$$F_c = qvB = m\frac{v^2}{r} \quad (5)$$

$$qBr = mv, \quad (6)$$

which combined with the angular momentum formula give two equations with two unknowns.

Solving for the unknowns

$$L = qBr^2 \quad (7)$$

$$r = \sqrt{\frac{L}{qB}} = 0.0500 \text{ m} \quad (8)$$

$$v = \frac{L}{mr} = 8.78 \text{ Mm/s}. \quad (9)$$

Problem 16. A wire $l = 2.80$ m in length carries a current of $I = 5.00$ A in a region where a uniform magnetic field has a magnitude of $B = 0.390$ T. Calculate the magnitude of the magnetic force on the wire assuming that the angle between the magnetic field and the current is (a) $\theta_a = 60.0^\circ$, (b) $\theta_b = 90.0^\circ$, and (c) $\theta_c = 120^\circ$.

Using our formula for the force on a wire due to a uniform field we have

$$\mathbf{F} = I\mathbf{l} \times \mathbf{B} \quad (10)$$

$$F = IlB \sin \theta, \quad (11)$$

so just plugging in

$$F_a = IlB \sin \theta_a = 4.73 \text{ N} \quad (12)$$

$$F_b = IlB \sin \theta_b = 5.46 \text{ N} \quad (13)$$

$$F_c = IlB \sin \theta_c = 4.73 \text{ N}. \quad (14)$$