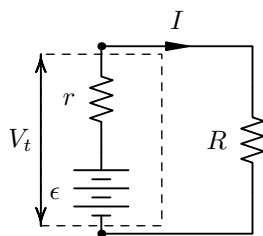


Homework 5

Chapter 21

Problem 25. A battery has an emf of $\epsilon = 15.0$ V. The terminal voltage of the battery is $V_t = 11.6$ V when it is delivering $P = 20.0$ W of power to an external load resistor R . (a) What is the value of R ? (b) What is the internal resistance r of the battery?



(a) Using the power absorbed by R

$$P = IV_t = \frac{V_t^2}{R} \quad (1)$$

$$R = \frac{V_t^2}{P} = \frac{(11.6 \text{ V})^2}{20.0 \text{ W}} = 6.75 \Omega \quad (2)$$

(b) The current through the entire circuit is given by

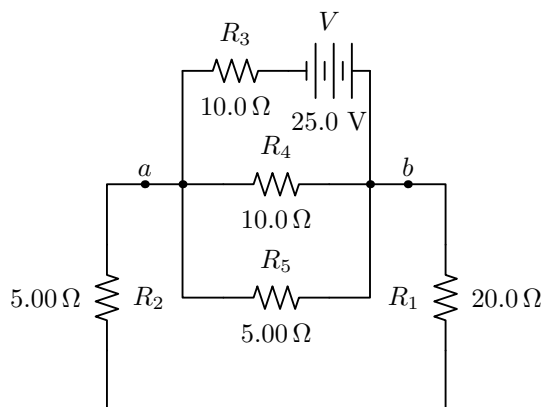
$$I = \frac{V_t}{R} = \frac{P}{V_t} = 1.72 \text{ A} \quad (3)$$

So the internal resistance is given by

$$\epsilon - V_t = Ir \quad (4)$$

$$r = \frac{\epsilon - V_t}{I} = \frac{3.4 \text{ V}}{1.72 \text{ A}} = 1.97 \Omega \quad (5)$$

Problem 29. Consider the circuit shown in Figure P21.29. Find (a) the current in the $R_1 = 20 \Omega$ resistor and (b) the potential difference between points a and b .



Label the voltage $V = 25.0$ V and the resistances (clockwise from b) $R_1 = 20.0 \Omega$, $R_2 = 5.00 \Omega$, $R_3 = 10.0 \Omega$, $R_4 = 10.0 \Omega$, and $R_5 = 5.00 \Omega$.

Computing some equivalent resistance of R_1 and R_2 in series we have

$$R_s = R_1 + R_2 = 25.0 \Omega \quad (6)$$

Computing the equivalent resistance of R_s , R_4 , and R_5 in parallel we have

$$R_p = \left(\frac{1}{R_4} + \frac{1}{R_5} + \frac{1}{R_s} \right)^{-1} = 2.94 \Omega \quad (7)$$

And the equivalent resistance of the entire setup is

$$R_e = R_p + R_3 = 12.94 \Omega \quad (8)$$

The total current is then (from Ohm's law)

$$I_e = \frac{V}{R_e} = 1.93 \text{ A} \quad (9)$$

And the voltage from a to b is

$$V_{ab} = I_e R_p = 5.68 \text{ V} \quad (10)$$

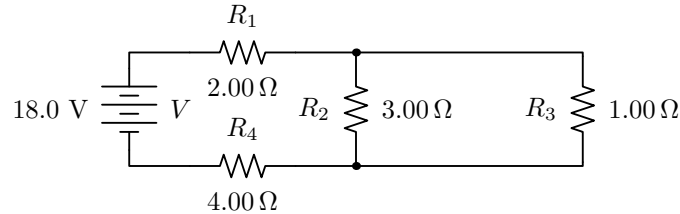
Which is what they were looking for in (b).

The current through the branch with R_1 and R_2 is then

$$I_s = \frac{V_{ab}}{R_s} = 227 \text{ mA} \quad (11)$$

Which is what they were looking for in (a).

Problem 31. Calculate the power delivered to each resistor in the circuit shown in Figure P21.31.



Label the voltage $V = 18.0 \text{ V}$ and the resistors (starting in the upper left) $R_1 = 2.00\Omega$, $R_2 = 3.00\Omega$, $R_3 = 1.00\Omega$, and $R_4 = 4.00\Omega$.

To find the total current through the circuit, we compute its equivalent resistance. First for the two resistors in parallel

$$R_p = \left(\frac{1}{R_2} + \frac{1}{R_3} \right)^{-1} = 0.750\Omega \quad (12)$$

And then for the complete circuit

$$R_c = R_1 + R_p + R_4 = 6.75\Omega \quad (13)$$

Using Ohm's law to calculate the total current $I_c = I_1 = I_4$ we have

$$I_c = \frac{V}{R_c} = 18/6.75 = 2.67 \text{ A} \quad (14)$$

And the powers dissipated through R_1 and R_4 are

$$P_1 = I_1 V_1 = I_c^2 R_1 = 14.2 \text{ W} \quad (15)$$

$$P_4 = I_c^2 R_4 = 28.4 \text{ W} \quad (16)$$

The voltage across R_p is given by

$$V_p = I_c R_p = 2 \text{ V} \quad (17)$$

And the powers dissipated through R_2 and R_3 are

$$P_2 = I_2 V_2 = \frac{V_p^2}{R_2} = 1.33 \text{ W} \quad (18)$$

$$P_3 = \frac{V_p^2}{R_3} = 4 \text{ W} \quad (19)$$