

**Midterm Exam**  
**(Date: Thursday, 2009/11/05, 11:00 AM–12:20 PM)**

1. Each residue in a peptide chain can adopt a range of conformations described by the  $\Psi$  and  $\Phi$  angles in the Ramachandran plot. Of the 20 naturally occurring amino acids, identify the amino acid that can adopt the largest range of  $(\Psi, \Phi)$  values. Which amino acid is characterized by the most restricted range of  $(\Psi, \Phi)$  values? Explain both choices.

**2.** The hydrogen bond between two water molecules in isolation is about ten times stronger energetically than a van der Waals contact between two xenon atoms, yet water molecules dimerize in the gas phase only about 30% more frequently than xenon atoms. Explain why.

**3.** The temperature at which the protein unfolds *increases* by 40°C when the water is removed either by dehydration or by transferring the protein to a non-aqueous solvent. What are the implications of this for the stability of protein folded conformations? Explain what happens to the free energy of a protein-protein hydrogen bond upon water removal.

4. Folding of a hypothetical protein is associated with a formation of a crucial metastable intermediate state I. What is the effect of an increased stability of this intermediate state,  $F_I \rightarrow F_I - \Delta F_I$ , on the folding rate? See the schematic figure. Express the transition time from unfolded to folded state in terms of the free energies in unfolded ( $F_U$ ), intermediate ( $F_I$  or  $F_I - \Delta F_I$ ), and folded ( $F_F$ ) states as well as the two free energy values at the top of the two barriers,  $F^{\#1}$  and  $F^{\#2}$ .

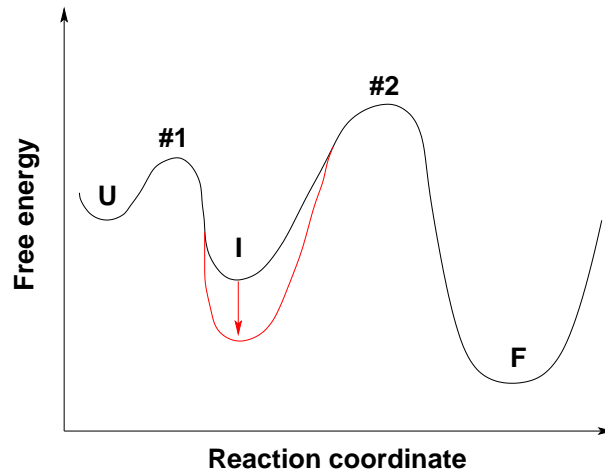


FIG. 1: Schematic picture of unfolded ( $U$ ), intermediate ( $I$ ), and folded ( $F$ ) state (Problem 4.)

5. A  $\text{Mg}^{2+}$  ion and a  $\text{Cl}^-$  ion are  $6\text{\AA}$  apart in water at  $25^\circ\text{C}$ . What is their electrostatic interaction energy in units of  $k_B T$ ? Debye-Hückel radius in water at physiological conditions is  $8\text{\AA}$ ,  $\epsilon_{eff} = 79$ , and  $\epsilon_0 = 8.85 \times 10^{-12} \text{ As/Vm}$ . How much stronger would this interaction be if the ions were two-times closer to each other?

**6.** A hypothetical protein is in unfolded state with the free energy  $F_U$ . Suppose that upon folding, the protein can adopt any of 5 transition states characterized by free energy values:  $F_1 < F_2 < F_3 < F_4 < F_5$ , where  $F_i > F_U$  for all  $i \in 1, 2, \dots, 5$ . Which of these states will contribute the most to the protein folding rate? Express the folding rate by the dominant term.

*(For honors undergraduate and graduate students.)*

7. Explain the origin of the change of the Gibbs free energy  $\Delta G$  of a hydrophobic molecule upon a transfer from vapor to water. Take into consideration that  $\Delta G$  consists of two contributions, (i) enthalpy change  $\Delta H$  and (ii) change in the entropic part  $T\Delta S$ ,  $\Delta G = \Delta H - T\Delta S$ .

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