

```

> # R. Gilmore
> # The generating function for Hermite polynomials is Taylor
expanded,
> # truncated at some finite order, and converted to a polynomial.
> # The successive derivatives are taken and evaluated at t=0.
> # The results are printed as the successive Hermite polynomials.
> #restart;
> GenHer:=exp(2*x*t-t^2);


$$GenHer := e^{2xt - t^2}$$


> nn:=10;

$$nn := 10$$


> h:=taylor(GenHer,t=0,nn+2);

$$- \left(-\frac{1}{3}x + \frac{2}{3}x^3 - \frac{4}{15}x^5 + \frac{8}{315}x^7\right)t^7 mbox{ } + \left(\frac{1}{24} - \frac{1}{3}x^2 + \frac{1}{3}x^4 - \frac{4}{45}x^6 + \frac{2}{315}x^8\right)t^8 + \left(\frac{1}{12}x - \frac{2}{9}x^3 + \frac{2}{15}x^5 - \frac{8}{315}x^7 + \frac{4}{2835}x^9\right)t^9 + \left(-\frac{1}{3}x + \frac{2}{3}x^3 - \frac{4}{15}x^5 + \frac{8}{315}x^7\right)t^{10} mbox{ } + \left(\frac{1}{24} - \frac{1}{3}x^2 + \frac{1}{3}x^4 - \frac{4}{45}x^6 + \frac{2}{315}x^8\right)t^{11} + \left(\frac{1}{12}x - \frac{2}{9}x^3 + \frac{2}{15}x^5 - \frac{8}{315}x^7 + \frac{4}{2835}x^9\right)t^{12} + \dots$$

> hh:=convert(h,polynom);

$$> hh:=taylor(GenHer,t=0,nn+2):H[0]:=subs(t=0,hh):print(0,H[0]);for i from 1 to nn do hh:=diff(hh,t):H[i]:=subs(t=0,hh):print(i,H[i]):od:$$

0, 1
1,  $2x$ 
2,  $-2 + 4x^2$ 
3,  $-12x + 8x^3$ 
4,  $12 - 48x^2 + 16x^4$ 
5,  $120x - 160x^3 + 32x^5$ 
6,  $-120 + 720x^2 - 480x^4 + 64x^6$ 
7,  $-1680x + 3360x^3 - 1344x^5 + 128x^7$ 
8,  $1680 - 13440x^2 + 13440x^4 - 3584x^6 + 256x^8$ 
9,  $30240x - 80640x^3 + 48384x^5 - 9216x^7 + 512x^9$ 
10,  $-30240 + 302400x^2 - 403200x^4 + 161280x^6 - 23040x^8 + 1024x^{10}$ 

```